

Calculations For Shrink Fitting

The amount that a particular metal will expand can be calculated using the coefficient of thermal expansion:

$$\delta = \alpha L(\Delta t)$$

δ = Total deformation desired (in or mm)

α = Coefficient of thermal expansion (in/in °F or mm/mm °C)

L = Nominal length of the part being heated (the diameter for a cylinder) (in or mm)

Δt = Temperature difference (°F or °C)

The coefficient of thermal expansion (α) for a particular metal can be found in Table 1.

The amount of holding stress developed once contraction of the outer hole has occurred can be calculated:

$$S_t = \frac{E * \Delta D}{4 * a} \left(1 + \frac{a^2}{b^2} \right) \quad S_r = \frac{E * \Delta D}{4 * a} \left(1 - \frac{a^2}{b^2} \right)$$

- S_t and S_r = Tangential and radial stresses developed between the collar and the shaft.
- 'a' and 'b' = Internal and external radii of the collar
- E = Elastic modulus

ΔD = Change of inner diameter of hole.

Table 1: Coefficient of Thermal Expansion and Elastic Modulus

Material	Coefficient of thermal expansion, α		Elastic Modulus (E) psi (at 70°F)
	In/in °F	mm/mm °C	
Steel:			
AISI 1020	6.5x10 ⁻⁶	11.7x10 ⁻⁶	30x10 ⁶
AISI 1050	6.1x10 ⁻⁶	11.0x10 ⁻⁶	29x10 ⁶
AISI 4140	6.2x10 ⁻⁶	11.2x10 ⁻⁶	
Stainless Steel:			
AISI 301	9.4x10 ⁻⁶	16.9x10 ⁻⁶	28.0x10 ⁶
AISI 430	5.8x10 ⁻⁶	10.4x10 ⁻⁶	29.0x10 ⁶
Aluminum:			
2014	12.8x10 ⁻⁶	23.0x10 ⁻⁶	10.5x10 ⁶
6061	13.0x10 ⁻⁶	23.4x10 ⁻⁶	
Bronze:	10.0x10 ⁻⁶	18.0x10 ⁻⁶	17x10 ⁶

* The elastic of modulus will decrease as temperature increases. At 1000°F, E, will be 22x10⁶ for steel.